The T- ρ coexistence curve of nuclear matter: EOS results

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In Fisher's droplet model [1] a non-ideal fluid is approximated by an ideal gas of droplets. Thus, summing over An_A , the normalized yield of droplets of size A multiplied by A, gives the density and the reduced density is:

$$\frac{\rho}{\rho_c} = \frac{\sum An_A(\Delta\mu, E_{Coul}, T)}{\sum An_A(\Delta\mu, E_{Coul}, T_c)}.$$
 (1)

With $\Delta\mu$ and E_{Coul} set to 0 in the numerator and $\Delta\mu$ and E_{Coul} set to 0 with T set to T_c in the denomenator, Eq. (1) gives the vapor branch of the coexistence curve of finite nuclear matter. Figure 1 shows the results from an analysis of the EOS fragment yields of 1 AGeV Au, La, Kr + C [1].

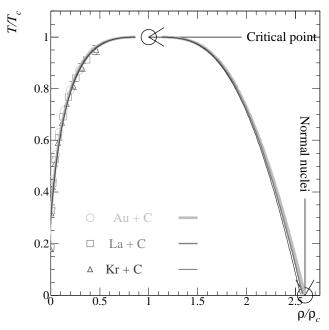


Figure 1: The points are calculations performed at the excitation energies below the critical point and the lines are a fit to and reflection of Eq. (2).

Following the work with simple fluids it is possible to determine the liquid branch as well: empirically, the ρ/ρ_c - T/T_c coexistence curves of

Table 1: EOS critical point values $T_c \, (\text{MeV}) \quad \rho_c \, (\rho_0) \quad p_c \, (\text{MeV/fm}^3)$ Au $7.6 \pm 0.2 \quad 0.39 \pm 0.01 \quad 0.11 \pm 0.04$ La $7.8 \pm 0.2 \quad 0.39 \pm 0.01 \quad 0.12 \pm 0.04$ Kr $8.1 \pm 0.2 \quad 0.39 \pm 0.01 \quad 0.12 \pm 0.04$

several fluids can be fit with the function:

$$\frac{\rho_{l,v}}{\rho_c} = 1 + b_1 (1 - \frac{T}{T_c}) \pm b_2 (1 - \frac{T}{T_c})^{\beta}$$
 (2)

where the parameter b_2 is positive (negative) for the liquid ρ_l (vapor ρ_v) branch. Fisher's droplet model gives $\beta = (\tau - 2)/\sigma = 0.3 \pm 0.1$ for this work [1]. With this value of β , fitting the coexistence curve with Eq. (2) gives a estimate of the ρ_v branch of the coexistence curve and changing the sign of b_2 gives the ρ_l branch, thus yielding the full T- ρ coexistence curve of finite nuclear matter.

Assuming that normal nuclei exist at the T = 0 point of the ρ_l branch of the coexistence curve, then using the parameterization of the coexistence curve in Eq. (2) gives ρ_c in Table 1.

The critical compressibility factor $C_c^F = p_c/T_c\rho_c$ can be determined from:

$$C_c^F = \frac{\sum n_A(\Delta\mu, E_{Coul}, T_c)}{\sum An_A(\Delta\mu, E_{Coul}, T_c)}.$$
 (3)

Performing these sums with $\Delta\mu$ and E_{Coul} set to 0 with T set to T_c gives $C_c^F = 0.3 \pm 0.1$ which agrees with the values for several fluids. Using the EOS T_c values [1] and ρ_c from above in combination with C_c^F gives a critical pressure, also shown in Table 1.

References

[1] J. B. Elliott *et al.*, to be submitted to Phys. Rev. C (2002).